



6a.  $g(4.5) = 13.5$ . This is the area under the graph of  $f$  in the first quadrant between  $x = 0$  and  $x = 4.5$ .

$g'(4.5) = f(4.5) = 0$ ;  $g''(4.5) = f'(4.5) = -2$ , the slope of the line segment containing  $(4.5, 0)$ .

6b. Average value of  $f$  equals  $\frac{1}{5 - (-3)} \int_{-3}^5 f(x) dx = \frac{1}{8} \left[ \int_{-3}^3 f(x) dx + \int_3^5 f(x) dx \right]$   
 $= \frac{1}{8} [27 + 2] = \frac{29}{8}$

The two integrals are found by finding the signed areas under the graph of  $f$ .

6c. There is a point of inflection where  $f$ , the derivative of  $g$ , has a maximum or minimum. This occurs only at  $x = 5$ , where  $f$  changes from decreasing to increasing, or where  $f'$  changes from negative to positive.

6d. The function  $g$  increases from  $x = -3$  to  $x = 4.5$ , then decreases until  $x = 7$ , and then increases again until  $x = 9$ . There is a maximum at  $(4.5, 13.5)$  (from part (a)). There is an endpoint maximum at  $x = 9$ . Use the signed area to find  $g(9)$ :

$$\begin{aligned} g(9) &= g(4.5) + \int_{4.5}^9 f(x) dx \\ &= 13.5 - 0.25 \end{aligned}$$

The endpoint maximum occurs at  $(9, 13.25)$ .